YANK: Free energy calculations made useful.

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Free energy: The view from pharma...

- Pharmaceutical research would love to have a fast accurate and reliable free energy tool.
- Usually the old engineering joke is fast accurate reliable, cheap, pick two...
- For free energy you get to pick one. If you are lucky.
- They've heard it all before. They live in the 'real world' apparently.



Ocker:

Software for discovery of inhibitors of protein-protein

ocker (slang)
noun

1. An oafish uncultured Australian man. Form: Ocker (often)

adj

1. Typical of an ocker; boorish; uncultured.

Etymology: 1970s: a form of the name Oscar, the name of a TV character.

Other: a name for a computational drug design program that was initially thought to be a clever play on DOCK, but seems less amusing now.





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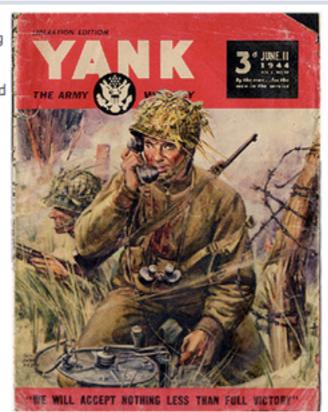
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Yank: Ligand binding free energy calculations in implicit solvent

Project Overview

Description Yank is a new code for estimating free energies of ligand binding using free energy perturbation and implicit solvent models, utilizing the OpenMM GPU-accelerated dynamics toolkit. While not as accurate as explicit solvent simulations, the myriad of advantages offered by implicit solvent (including constant pH treatments) and speed advantages offered by GPU acceleration are expected to provide significant utility for medicinal chemists.



Purpose/Synopsis

Provide a computational

tool for rapidly estimating protein-ligand binding free energies using implicit solvent models

Audience Molecular modelers interested in virtual screening methods for identification of small molecule ligands of biomolecules

Long Term Goals and Related Uses Provide a computational tool for rapidly estimating protein-ligand binding free energies using implicit solvent models

Project Lead



John Chodera Contact



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The drug development cycle

- Identify the therapeutic target
- Find from (biopiracy, patents, screening [uHTS, virtual], academia) a lead compound.
- Develop lead compound to have appropriate potency for the target, selectivity, and pharmacokinetic and metabolic profiles
- Ideally its a short synthesis with no stereo centres, and has a single crystal allomorph.
- Formulate and hand it over to the crack team of cheerleaders and bribery experts we call pharmaceutical sales.... *

^{*} except at vertex, because we are ethical...

So where would we use free energy?

potency

selectivity / DPMK

formulation

- Of the hundreds of derivatives I could make, which one should I make? Ranking congeneric series is very hard
- Should I put a stereocenter in? will this give me selectivity?
- Can I lock in a tautomeric state? Will this help me? Is this a bio-isostere?
- How can I make a change to avoid a metabolic liability and not loose potency?
- What are the most stable crystal forms for this molecule?
- What is the solubility of the molecule from each crystal form?

This free energy you speak of, is it fast?

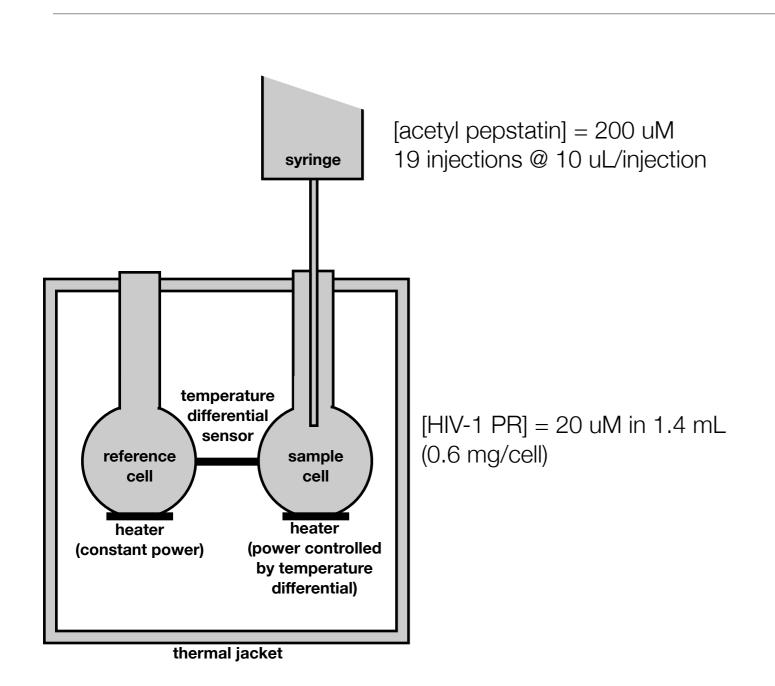
- No. Not currently.
- Yeah we tried that ages ago, took a long time and didn't work
- "I'm never writing AMBER inputs again."
- But I can just do the experiment and have the 'right answer".
- Takes too long. I get paid to make molecules!

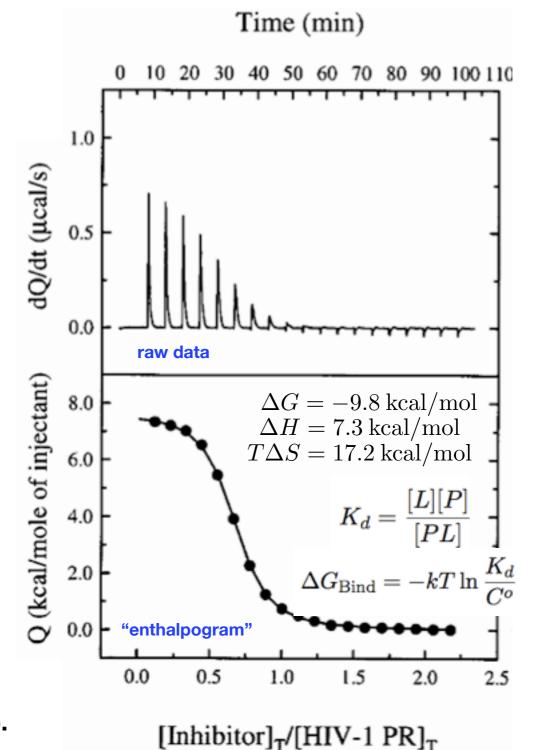
In short: We need to turn around an accurate free energy calculation in a day.

The aim of YANK: Fast, accurate binding free energies in a day.

- At Vertex we deploy tools in two forms. "EZ" such as "EZDock" or "EZSim"
- This allows chemist to perform their own calculations. "Professional" modelers use more detailed tools for project specific support.
- If we can do a compound a day on a GPU, we can easily scale this up by using more GPU's/ compound.
- Having an actual energy function that is fast and works would allow alot of useful modeling that we currently don't do.. (Computational fragment screening, maybe making docking work better than ligand based methods)
- Chemists might start with the most soluble lead, rather than the most potent one if they were confident they could easily build in potency. (They always use the most potent one, because its hard to say to your manager, "we've got great ADME/Tox we just need to work on the potency....")

Binding affinities can be (in)directly measured by experiment





Simultaneously provides estimates of both ΔG and ΔH (and hence $T\Delta S$).

(Note that some reactions have no measurable change in heat, and are not measurable by ITC.)

Binding affinities can be directly computed through equivalent alchemical thermodynamic cycles

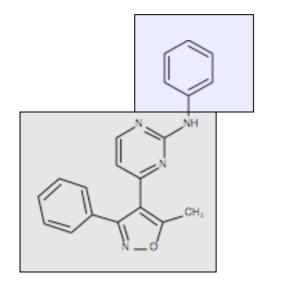
Relative free energies of binding

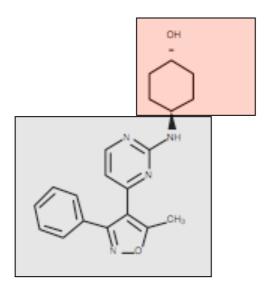
$$P+L_{1} \xrightarrow{\Delta G_{1}} PL_{1}$$

$$\Delta G_{a} \downarrow \qquad \qquad \downarrow \Delta G_{b}$$

$$P+L_{2} \xrightarrow{\Delta G_{2}} PL_{2}$$

$$\Delta \Delta G = \Delta G_a - \Delta G_b$$





Absolute free energies of binding

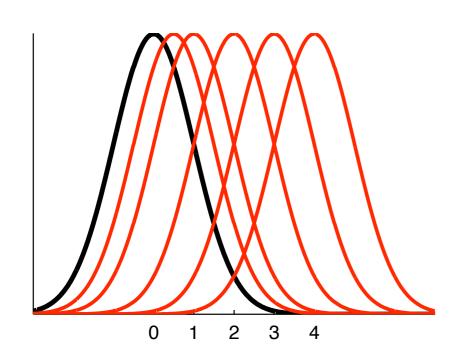
$$P + L \xrightarrow{\Delta G_{\text{bind}}} PL$$

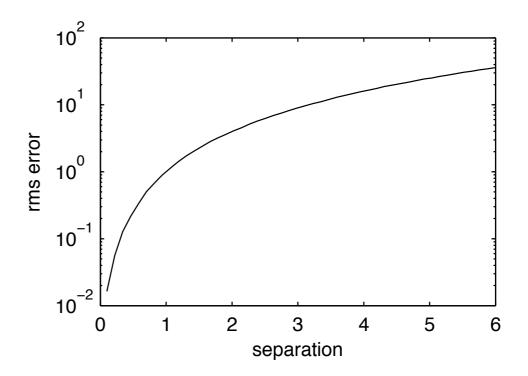
$$\downarrow \qquad \qquad \uparrow$$

$$P + \emptyset \longrightarrow P\emptyset$$

Alchemical intermediates can facilitate convergence

Error increases rapidly with diminishing phase space overlap



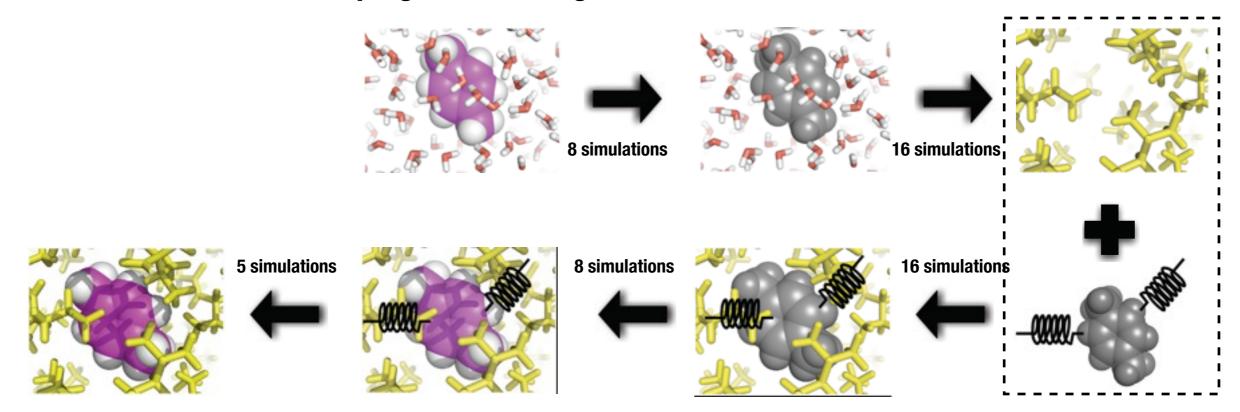


Instead, introduce intermediate states to ensure a contiguous chain of good overlap

$$\Delta F_{1\to N} = -\beta^{-1} \ln \frac{Z_N}{Z_1} = -\beta^{-1} \ln \frac{Z_2}{Z_1} \cdot \frac{Z_3}{Z_2} \cdot \dots \cdot \frac{Z_N}{Z_{N-1}} = \sum_{n=1}^{N-1} \Delta F_{n\to n+1} \qquad Z_n = \int d\mathbf{x} \, e^{-\beta U(\mathbf{x})}$$

Absolute alchemical free energy calculations involve simulations at multiple thermodynamic states

Alchemical transformation progresses through a number of intermediates



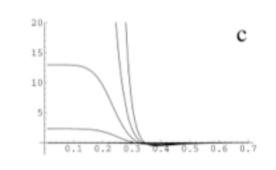
Free energy differences for each step are estimated from equilibrium simulations of intermediates

electrostatic annihilation

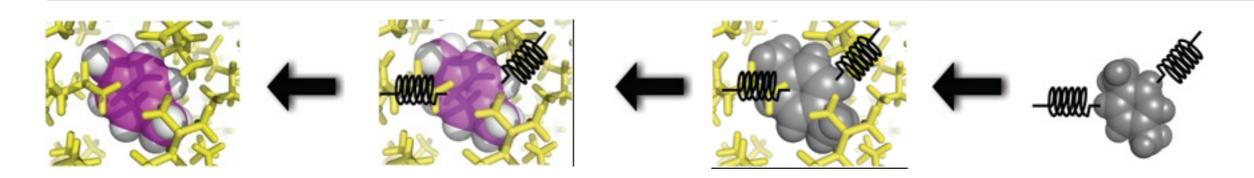
Lennard-Jones decoupling

$$q_i \rightarrow \lambda_{elec} \cdot q_i$$
 (for ligand charges)
$$U_{ij}^{\mathbf{L}}(r^{ij};\lambda) = \lambda^n 4\epsilon_{ij} \left(\frac{1}{[\alpha_{\mathbf{L}}(1-\lambda)^2 + (r_{ij}/\sigma_{ij})^6]^2} - \frac{1}{\alpha_{\mathbf{L}}(1-\lambda)^2 + (r_{ij}/\sigma_{ij})^6} \right)$$

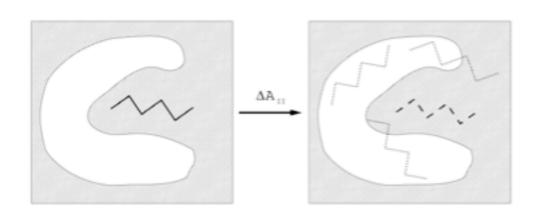
(for ligand-environment interactions)



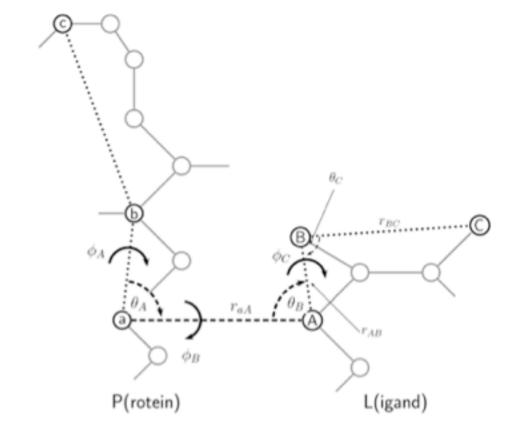
Restraints are used to aid convergence



Without restraining ligand in binding pocket, would need to sample entire simulation box at each discharging/decoupling intermediate



Choice of atoms to restrain is arbitrary in principle, minor practical differences among choices



Free energy differences can be estimated in several ways

TI (thermodynamic integration)

$$\Delta F = \int_{\lambda_1}^{\lambda_2} d\lambda' \left\langle \frac{\partial H}{\partial \lambda} \right\rangle_{\lambda'} \approx \frac{\Delta \lambda}{2} \left[\left\langle \frac{\partial H}{\partial \lambda} \right\rangle_{\lambda_1} + \left\langle \frac{\partial H}{\partial \lambda} \right\rangle_{\lambda_2} \right]$$

quadrature error difficult to quantify

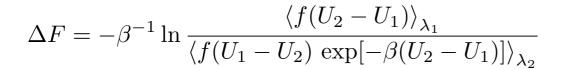
EXP (exponential reweighting)

$$\Delta F = -\beta^{-1} \ln \left\langle e^{-\beta(U_2 - U_1)} \right\rangle_{\lambda_1} = +\beta^{-1} \ln \left\langle e^{-\beta(U_1 - U_2)} \right\rangle_{\lambda_2}$$

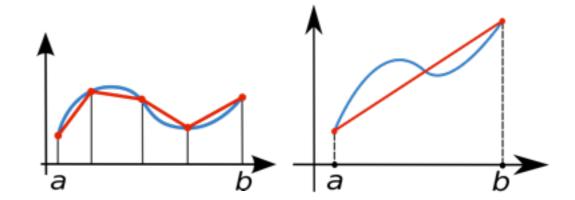
Zwanzig RW. *JCP* **22**:1420, 1954. Shirts MR and Pande VS. *JCP* **122**:144107, 2005.

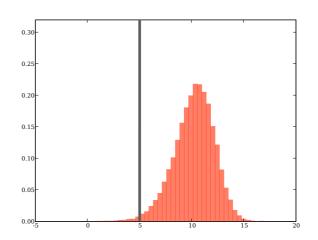
suffers from large bias and variance

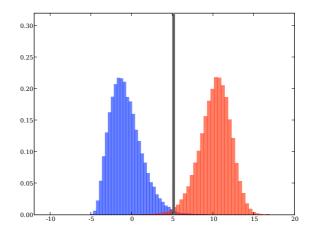
BAR (Bennett acceptance ratio)



Bennett CH. *J Comput Phys* **22:**245, 1976. Shirts MR, Bair E, Hooker G, and Pande VS. *PRL* **91:**140601, 2003.

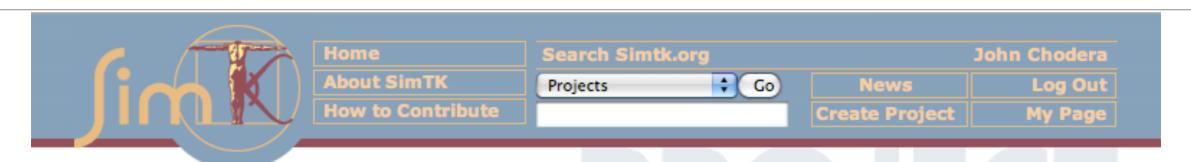






Python implementation of MBAR available now at

http://simtk.org/home/pymbar



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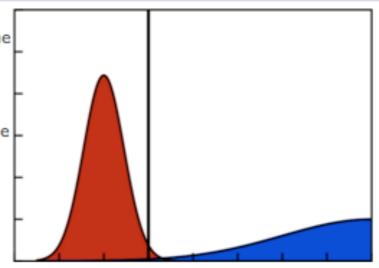


https://simtk.org/home/pymbar

pyMBAR: A Python implementation of the multistate Bennett acceptance ratio

Overview

A Python implementation of the multistate Bennett acceptance ratio (MBAR) method for estimation of expectations and free energy differences (and their statistical uncertainties) from multiple equilibrium simulations at different thermodynamic states.



Project Lead



John Chodera Contact



Michael Shirts Contact

Purpose Analyze data from multiple equilibrium simulations at different thermodynamic states

Audience Computational chemists and statistical physicists

Long Term Goals and Related Uses This project provides a Python reference implementation of the multistate Bennett acceptance ratio (MBAR) method for the analysis of multiple equilibrium simulations at different thermodynamic states Principal Downloads

pyMBAR 0.91 beta

pymbar-examples 0.91 beta

See All Downloads

Checklist of potential concerns in binding calculations

Protein conformation

Which conformation is most likely?
Conformational change upon binding
Multiple conformations contributing to binding

Post-translational modifications

Phosphorylation, glycosylation, acylation, alkylation

Protein protonation state

Appropriate choice of protonation state Change in protonation state upon binding Mixture of protonation states relevant to binding

Appropriate choice of protonation/tautomeric state Change in protonation/tautomeric state upon binding Mixture of protonation/tautomeric states relevant to binding

Ligand protonation/tautomeric state

$$-C$$
 H_2
 NH
 NH
 H^+

Salt environment

Salt required for function Appropriate salt parameters Other cosalts, cosolvents, and chelators

$$NaCl \longrightarrow MgCl_2$$

Checklist of potential concerns in binding calculations

Ligand parameter assignment

Anecdotal reports of Antechamber issues

Protein forcefield choice

parm96 deprecated; parm03 unvalidated for free energies

modified amino acid parameters

Don't have time to rederive appropriate Only found parameters for parm99

cofactors or other peptides bound?

Simulation timescales

Can we converge estimates for even a single conformation state?



http://amber.scripps.edu/antechamber/

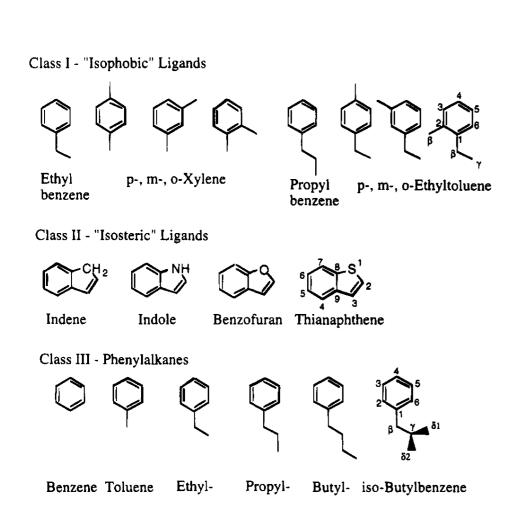
FEAMBER

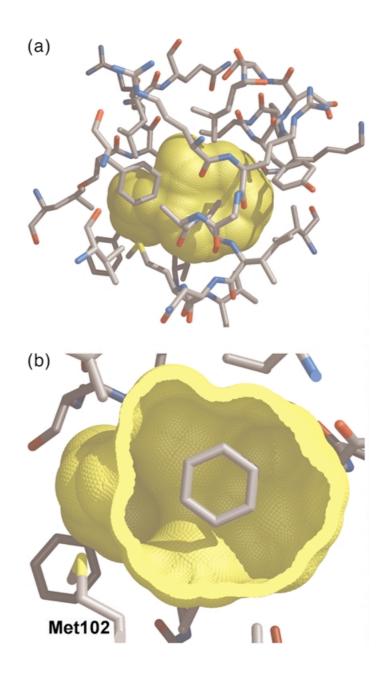
ffamber96, ffamber99sb, ffamber03 http://chemistry.csulb.edu/ffamber/

AMBER parameter database

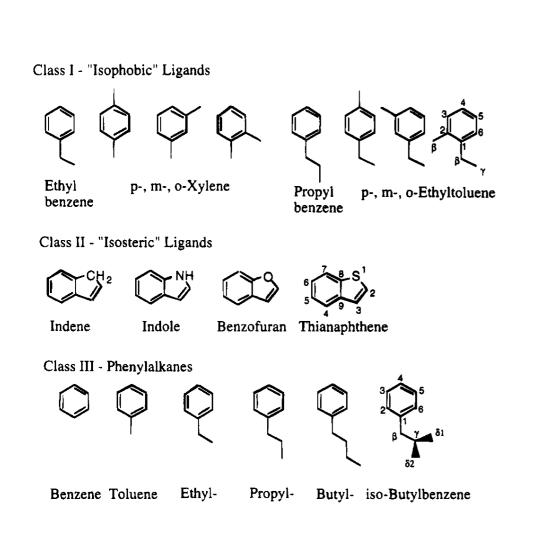
http://www.pharmacy.manchester.ac.uk/bryce/amber

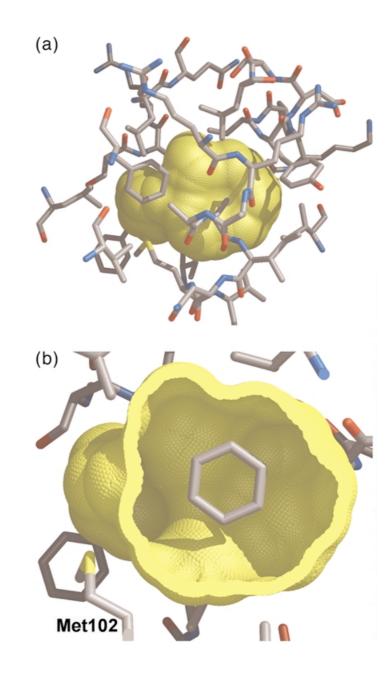
T4 lysozyme L99A: A model binding site for small hydrophobic ligands



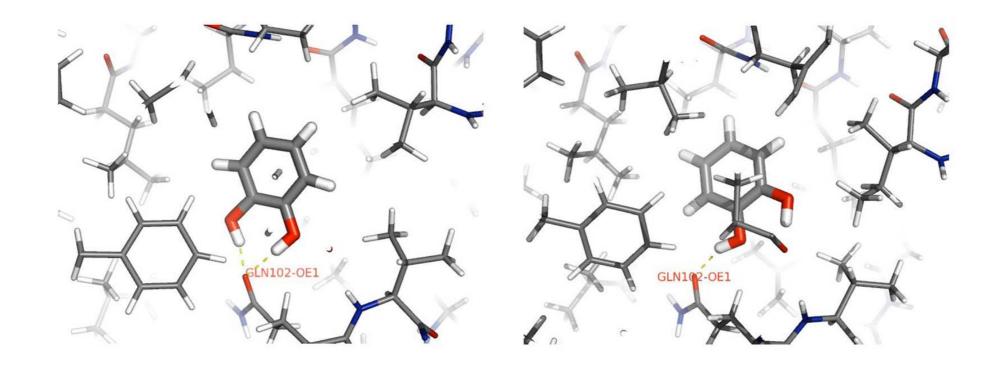


T4 lysozyme L99A: A model binding site for small hydrophobic ligands



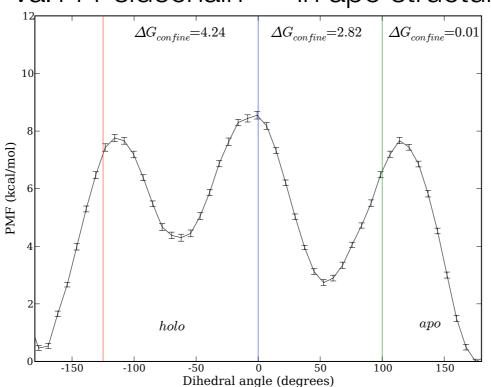


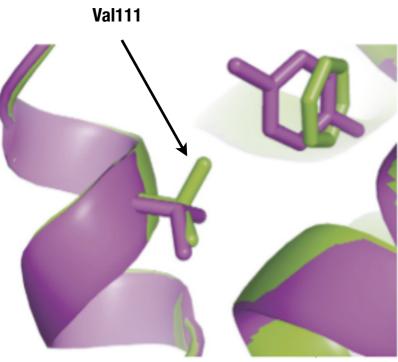
Can we quantitatively predict binding affinity of known ligands?



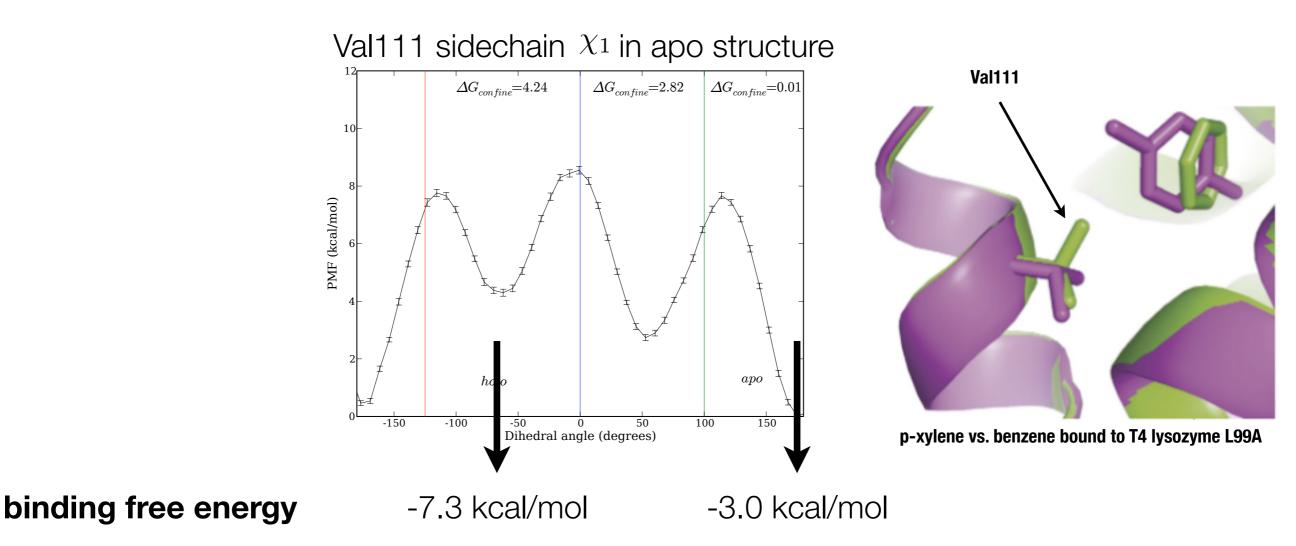
Difference in affinity between different bound orientations is only ~1 kT

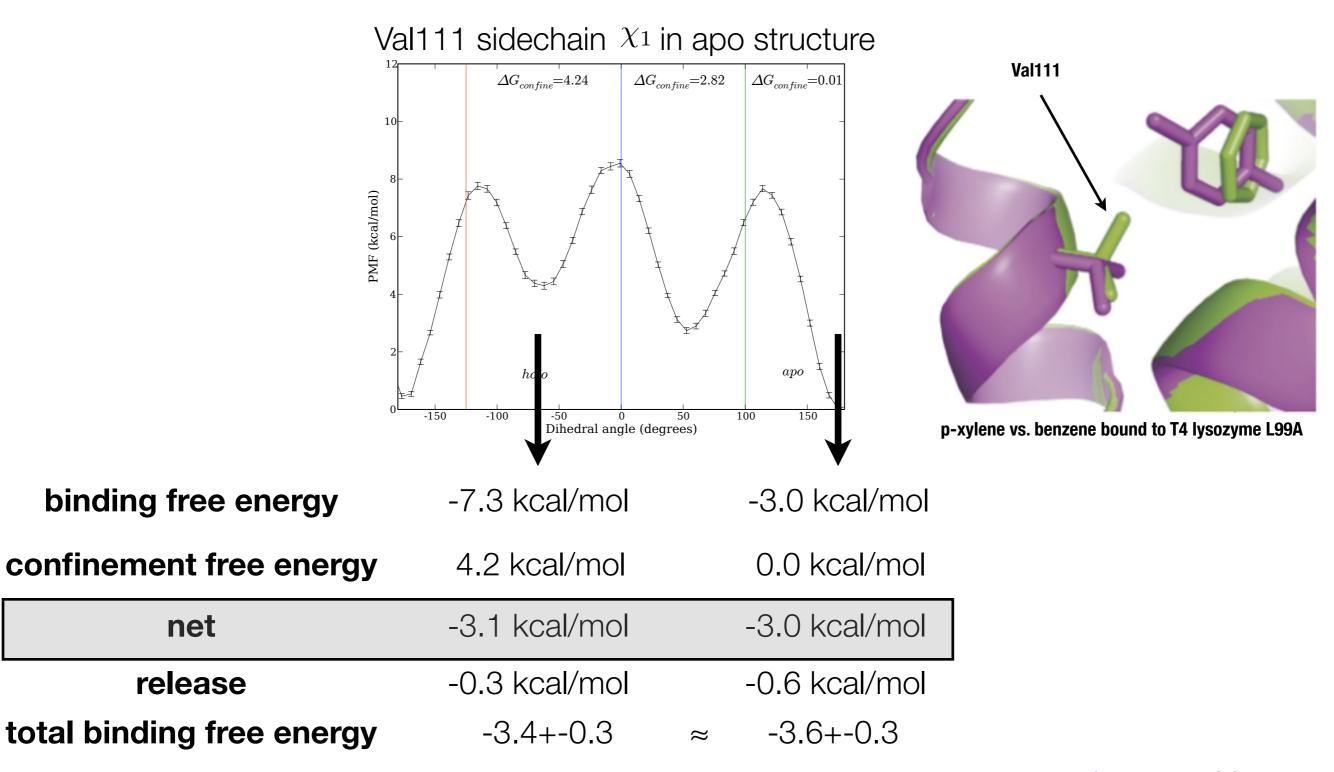
Val111 sidechain χ_1 in apo structure





p-xylene vs. benzene bound to T4 lysozyme L99A

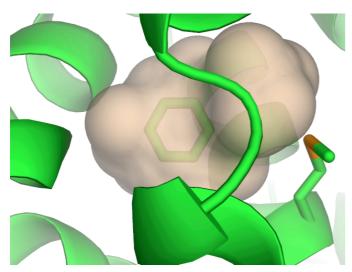




How accurately can we reproduce known binding affinities?

Retrospective test on known, neutral small-molecule ligands of T4 lysozyme L99A

only apo structure was used



model binding site in T4 lysozyme L99A

Ligand	$\Delta G_{expt.}^{o}$	$\Delta G_{calc.}^{o}$	$\Delta G_{calc.}^o - \Delta G_{expt.}^o$				
	kcal/mol	kcal/mol	$\rm kcal/mol$				
2,3-benzofuran	-5.46 ± 0.03	-3.53 ± 0.06	1.93 ± 0.07				
benzene	-5.19 ± 0.16	-4.56 ± 0.20	0.63 ± 0.26				
ethylbenzene	-5.76 ± 0.07	-6.36 ± 0.18	-0.60 ± 0.19				
indene	-5.13 ± 0.01	-1.75 ± 0.07	3.38 ± 0.07				
indole	-4.89 ± 0.06	-0.42 ± 0.08	4.47 ± 0.10				
isobutylbenzene	-6.51 ± 0.06	-5.01 ± 0.20	1.50 ± 0.21				
n-butylbenzene	-6.70 ± 0.02	-4.87 ± 0.14	1.83 ± 0.14				
n-propylbenzene	-6.55 ± 0.02	-5.88 ± 0.11	0.67 ± 0.12				
o-xylene	-4.60 ± 0.06	-1.27 ± 0.18	3.33 ± 0.19				
p-xylene	-4.67 ± 0.06	-3.54 ± 0.17	1.13 ± 0.18				
toluene	-5.52 ± 0.06	-4.58 ± 0.12	0.94 ± 0.14				
phenol	> -2.74	-1.26 ± 0.09	N/A				
2-fluorobenzaldehyde	> -2.74	-2.92 ± 0.14	N/A				
RMS error:		2.24					
Correlation, R :		0.72					

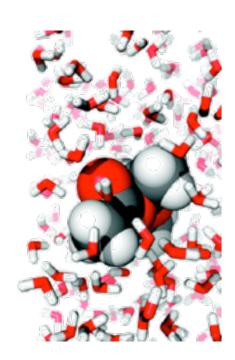
How accurately can we predict unknown binding affinities?

Ligand	DOCK Score	Prediction ¹	ΔG_{calc}^{o-2}	ΔT_m	Experiment	$\Delta G_{expt.}^{o}$
	(kcal/mol)		(kcal/mol)	(°C)		(kcal/mol)
1,2-dichlorobenzene	-19.99	Binder	-5.66 ± 0.15	2.90	Binder	-6.37
n-methylaniline	-17.29	Binder	-5.37 ± 0.11	1.00	Binder	-4.70
1-methylpyrrole	-15.27	Binder	-4.32 ± 0.08	2.20	Binder	-4.44
1,2-benzenedithiol	-18.51	Binder	-2.79 ± 0.13	2.50	Binder	N.D.
thieno-[2,3-c]pyridine	-18.81	Nonbinder	-2.56 ± 0.07	-0.40	Nonbinder	N.D.

T-1-1- 1

prediction accuracy ~ 0.5 kcal/mol

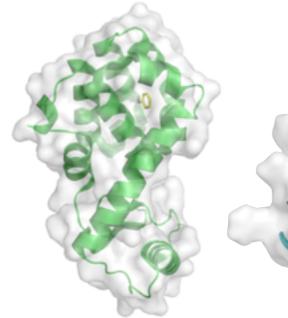
How far are we toward targets relevant to pharma?



hydration free energies of small neutral molecules

1.23±0.01 kcal/mol [502] (Mobley et al., 2008)

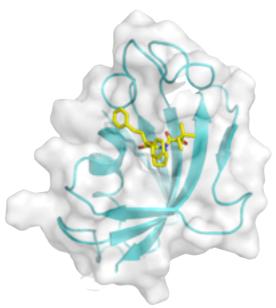
1.33±0.05 kcal/mol [17]
(Nicholls and Mobley et al., J Med Chem)



small apolar ligands T4 lysozyme L99A

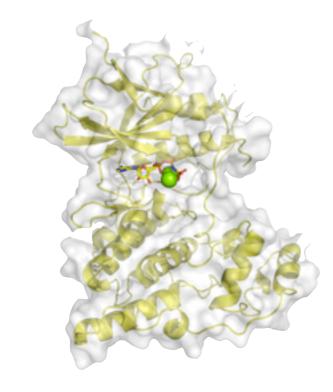
1.89±0.04 kcal/mol [13] (Mobley and Graves et al., JMB 2007)

0.6±0.2 kcal/mol [3] (Mobley and Graves et al., JMB 2007)



polar ligands FKBP12

1.42 kcal/mol [9] 0.94 kcal/mol [7] (Shirts et al., in preparation)



JNK3 kinase

Specific goals for YANK

Accelerate free energy calculations on commodity GPUs using OpenMM

The other extreme is Anton: an expensive, special-purpose machine for MD.

Test how accurate implicit solvent models are for ligand-binding free energy calculations Largely unknown, only ~2 papers: Essex J Med Chem 49:7427, 2006; Roux Proteins 74:996, 2009.

Determine how critical statistical mechanics is for "rescoring" docked poses

Many rescoring methods use GB models, but all focus on energies of minimized conformations

Make free energy calculations both more realistic and more "idiot-proof"

Automatic sampling of protonation states, tautomers, salt concentrations

Provide a testbed for enhanced sampling algorithms that mix Monte Carlo and MD Mix in efficient Monte Carlo moves; exploit Markov chain Monte Carlo algorithms

Build a tool for pharma and academia that fills a special "niche" between dock/rescore and FEP Aim to replace unreliable, deficient methods like GB rescoring, MM-PBSA, MD

Alchemical free energy calculations have stricter requirements than "typical" MD applications

"My simulations is fine as long as gromacs didn't segfault [too many times]" is not sufficient.

Free energies often exquisitely sensitive to details that seem "unimportant" in straightforward MD: e.g. choice of PME parameters, long-range dispersion corrections, polarization convergence tol

What we need from OpenMM:

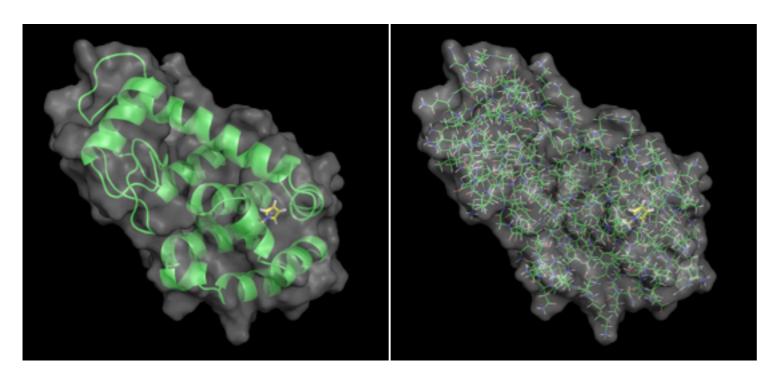
Correct equilibrium must be sampled in order for relationships used in estimating free energy differences (e.g. BAR) to provide a meaningful estimate:

forces must be accurate derivatives of potential integrator and thermostats must generate correct ensemble

Potential energy differences between alchemical states must be computed precisely e.g. early versions of gromacs used single-precision accumulators for PME energy

Milestone 1 : Feasibility Does OpenMM provide sufficient speed and accuracy?

Implement AMBER crd/prmtop reader
Test energy conservation and timing for a "real system" where only change is GB model



T4 lysozyme L99A + 1-methylpyrrole [2616 atoms]
AMBER parm96 / GAFF + AM1-BCC charges
same system treated by Mobley et al.
except OBC GBSA instead of explicit solvent

also, test on more realistic systems:

- trypsin inhibitors [charged ligands]
- CDK2 kinase [real target]

Conditional pass

Erroneous force computation on NVIDIA GeForce 9600M GT and GeForce GT 120, despite passing all CUDA and OpenMM tests. Only obvious with force calculations or constant-energy simulations; wouldn't notice a problem with NVT simulations until your protein started to unfold!

NVIDIA GeForce GTX 285 gives correct forces and stable NVE dynamics with ~ 32 ns/day performance Compare to Intel Core 2 Duo 2.4 GHz with single-core performance ~ 36 ps/day!

Milestone 2: Accuracy of GBSA models How much additional error is introduced by use of GBSA?

Repeat same free energy calculations as Mobley at al. for T4 lysozyme and other systems Determine how much GBSA model degrades performance

Just need code fast enough for comparison to be feasible -- optimize later.

scale charges and GB intrinsic radii:

$$q_i \rightarrow (1 - \lambda_{elec}) \cdot q_i$$

$$\sigma_i^{GB} \rightarrow (1 - \lambda_{elec}) \cdot \sigma_i^{GB}$$

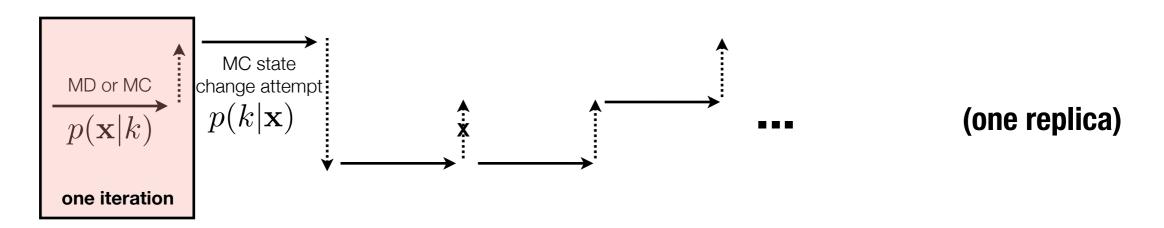
no soft-core support, so scale LJ radii and well depth:

$$\sigma_i \to (1 - \lambda_{LJ}) \cdot \sigma_i$$
 $\epsilon_i \to (1 - \lambda_{LJ}) \cdot \epsilon_i$

Basic algorithm for free energy calculations:

```
for each alchemical state k = 1:K
  for each iteration n = 1:N
    integrate T steps of dynamics with thermostat
    for each alchemical state l = 1:L
        compute potential energy of current configuration at state l and store it
reprocess all data with MBAR
```

Replica-exchange can reduce correlation times and provides a "built-in" convergence estimate



Original algorithm:

```
for each alchemical state k = 1:K
  for each iteration n = 1:N
    integrate T steps of dynamics with thermostat
    for each alchemical state l = 1:L
        compute potential energy of current configuration at state l and store it
reprocess all data with MBAR
```

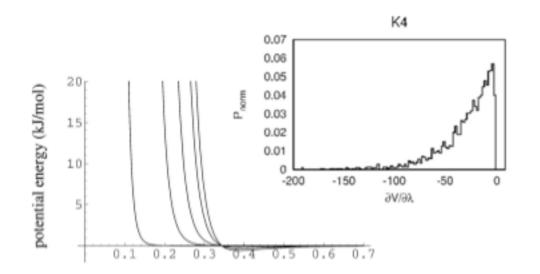
New algorithm:

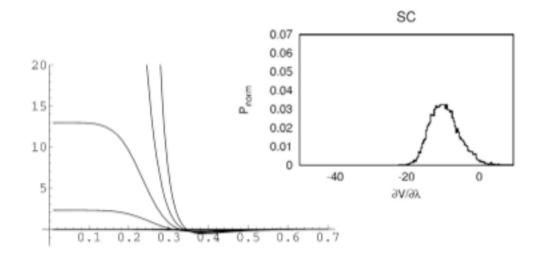
```
for each iteration n = 1:N
  for each replica k = 1:K
    mix states among replicas (Gibbs sampling)
    integrate T steps of dynamics with thermostat
    for each alchemical state l = 1:L
        compute potential energy of current configuration at state l and store it
reprocess all data with MBAR
```

If each replica initialized from a different conformation (e.g. docked pose, receptor model), we have a "built-in" convergence check: Calculation is only converged after estimates of binding affinity from all replicas agree within statistical error.

Milestone 3: Critical efficiency / usability improvements

Soft-core Lennard-Jones interactions critical to reducing variance in estimated free energies in explicit solvent calculations; likely important for implicit as well.





Steinbrecher T, Mobley DL, and Case DA. JCP 127:214108, 2007. Pitera JW and van Gunsteren WF. Mol. Sim. 28:45, 2002.

Could potentially be implemented with lookup tables, which also allows "fused" intermediates [e.g. Beutler and van Gunsteren JCP 101:1417, 1994].

GPU-accelerated energy calculations to reduce bottleneck

Kai is near nearly finished with these

Automatic ligand parameterization / system setup scripts Switch to Python codebase

Critical for programmer efficiency; sanity
Will require near-complete exposure of OpenMM API
Helping out Randy with pyOpenMM: https://simtk.org/home/pyopenmm

Milestone 4: Treating realistic systems, making calculations "idiot-proof", enhancing sampling

Constant-pH simulations

Easily implemented in GB via simple Monte Carlo moves where proton parameters are modified. [Mongan et al. J Comput Chem 25:2038, 2004.]

Debye-Hückel screening for monovalent counterions

Already incorporated into AMBER GB models [Srinivasan et al. Theor. Chem. Acc. 101:426, 1999]

Monte Carlo sampling of tautomers

If aqueous tautomer ratios are known or can be predicted, MC moves allow switches between

Semi-grand-canonical sampling of divalent (or all explicit) counterions?

Easily implemented in MCMC framework

Efficient torsion MC moves for sampling sidechain conformational changes

e.g. "smart-darting MC", with move set of rotamer displacements [JCP 114:6994, 2001]

All of these methods simply are different MC moves that "plug in" to the same MCMC framework.

Milestone 5 and beyond

Integrated setup pipeline

There's no reason we can't incorporate the entire MODELLER + MCCE pipeline we use to build in missing residues and heavy atoms and select protonation states.

Markov state models

One way to overcome slow conformational dynamics of proteins: Divide-and-conquer Related to concepts of "conformational selection"

Expanded-ensemble methods for sampling over huge libraries of compounds

Find the best binders in a combinatorially-constructed library

Enhanced sampling methods such as NML

Collaborators and funding

Stanford

Vijay Pande Imran Haque

Vertex

Kim Branson Pat Walters

Mark Murcko

Stanford SimBios

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University of Virginia

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David Mobley



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California Institute for Quantitative Biosciences (QB3) Distinguished Postdoctoral Fellowship

The standard state for binding free energies

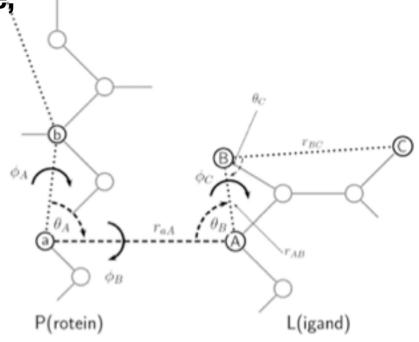
Association constant is not unitless:

$$K_a = \frac{[PL]}{[P][L]} = \frac{e^{-\beta \Delta G_a}}{(1 \text{ M})}$$

Free energy of binding is defined with respect to a reference state Standard reference state is 1M ligand (1 ligand / 1660 A³)

Luckily, if you use Boresch's ligand restraints to aid convergence, he has already computed the free energy correction for you!

$$\Delta A_{\rm r}^{\rm VBA,0} = -kT \ln \left[\frac{8\pi^2 V^0}{r_{\rm aA,0}^2 \sin \theta_{\rm A,0} \sin \theta_{\rm B,0}} \frac{(K_{\rm r} K_{\theta_{\rm A}} K_{\theta_{\rm B}} K_{\phi_{\rm A}} K_{\phi_{\rm B}} K_{\phi_{\rm C}})^{1/2}}{(2\pi kT)^3} \right]$$

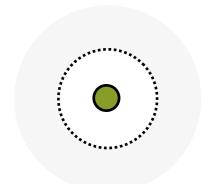


Anisotropic long-range dispersion correction

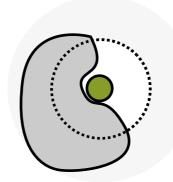
Simulations in solvent must be run with long-range dispersion correction to ensure results are not sensitive to choice of cutoff.

; Apply long range dispersion corrections for Energy and Pressure = DispCorr = AllEnerPres

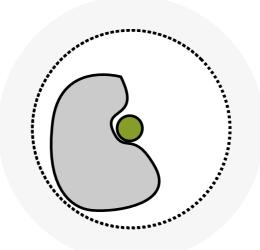
This correction assumes isotropic distribution of Lennard-Jones sites throughout system.



isotropic assumption holds



isotropic assumption fails



isotropic assumption holds

Instead, we have to enlarge cutoff so that isotropic assumption holds

An explicit postprocessing step recomputes energies with large cutoff and estimates perturbation free energies using EXP.

Can make a difference of 3 kcal/mol, depending on number of ligand atoms